## 颱風波를 基準으로한 全設計水深의 算定에 關한 硏究

## 李 重 雨

# A Study on the Calculation of Total Design Water Depth from Typhoon Waves

Joong-Woo, Lee\*

..... CONTENTS .....

- 1. INRTODUCTION
- 2. EQUATIONS FOR TYPHOON PARAMETER
  - 2.1. Equation for Pressure Profile Model
  - 2.2. Equations for Prediction of Hurricane Wind Fields
  - 2.3. Equations for Prediction of Hurricane Wave Fields
  - 2.4. Determination of Typhoon Parameters for Typhoon Brenda
- 3. CALCULATION OF THE 100-YEAR DESIGN WAVE PARAMETERS
  - 3.1. Description of Study Area
  - 3.2. Calculation of Typhoon Parmeters
  - 3.3. Analysis of S.S.M.O. and Hogben & Lumb's Wave Data
- 4. CALCULATION OF TOTAL DESIGN WATER DEPTH
- 5. SUMMARY AND DISCUSSIONS

REFERENCES

#### **Abstract**

Various typhoon data near Youngil Bay, Korea from 1961 to 1985 were collected with some criteria and analyzed with the help of the computer. Introducing the pressure profile models and predicting the typhoon wind and wave fields, the 100-year design wave parameters were calculated. Additionally, the wave data at the southeast coast of Korea were statistically analyzed.

The deep water wave climate of this bay indicated that Typhoon Brenda, 1985 had wave

<sup>\*</sup> Member, Department of Port and Transportation Engineering, Korea Maritime University

characteristics of 100-year return period. Typhoon model and storm surge model studies were made for this typhoon.

These, including other design parmeters, were introduced into the calculation of total design water depth.

## 要 約

컴퓨터를 이용하여 1961년에서 부터 1985년까지 한국 영일만 부근의 여러 颱風資料를 特定 設定 基準에 따라 수집하여 분석하였다. 壓力 斷面 모델을 도입하여 태풍에 의한 바람과 波浪海域을 예측하고 100년 設計波의 파라메타를 계산하였다. 또한 한국 남동해안의 波浪에 대한 자료를 통계적으로 분석하였다.

영일만에 대한 深海波分析으로는 1985년의 颱風 Brenda가 100년 回歸週期를 가진 것으로 나타나 태풍모델과 暴風海溢 모델을 통해 이를 조사하였다. 다른 設計파라메타와 함께 조사된 자료는 全 設計水深의 算定에 도입되었다.

## 1. Introduction

There is no doubt as to the destructive character of tropical storms, whereas an even more destructive and significant fraction of total storm damage is the storm generated surge and waves.

Storm surge and its impact of the coastal regions have been of interests to many researchers and engineers for a long time. It is a very inportant factor in producing barrier-island washovers and breaching. Especially, the storm surges have their greatest impacts in the coastal areas that experience such storms and are topographically low lying. During periods of extreme storm activity, low lying coastal areas may be flooded and overwashed by sea water.

The reliable estimates of the water

level changes during the storm conditions are essential to coastal planning and design. However, the decision of water level elevations under storms is a complicate problem which is involved in the interaction between wind, water, differences in atmospheric pressure, and other effects unrelated to the storm.

The purpose of this study is to predict storm wave conditions with a numerical model by the analysis of the past typhoon data and to calculate the total water depth for design of a shore structure at the selected site. The selected site is the Youngil Bay, Korea.

#### 2. Equations for Typhoon Parameter

Several references are available for the development of various hurricane



models and how to choose a particular model based upon certain hurricane parameters. The important parameters which had shown a good agreement among the various models are: a)  $R_{c'}$ , the radius of maximum cyclostrophic wind, b)  $P_{RC}$ , the pressure at the radius of maximum cyclostrophic wind, and c)  $\left(\frac{rdP}{dr}\right)_{max}$ , the maximum value of gradient of pressure multiplied by r.

## 2.1. Equation for Pressure Profile Model

There are several pressure profile models from the various sources. Those are proposed by Schloemer (1954), Fujita (1962), Jelenianski (1966). Uji (1975), Schwerdt, Ho and Watkins (1979), Holland (1980), Bretschneider (1981, 1982), and Rosendal (1982), etc.

In general, these can be summarized as two main groups: 1) the modified Rankin Vortex Model by Holland (1980). of which the Hydromet Model is a special case, and 2) the BRET-General Model of which the BRET-X Model, the Fujita model and Jelenianski Model are all special cases.

The mathematical expression of these two groups are:

$$\frac{P_r - P_o}{P_r - P_o} = Ae^{-B\frac{R_c}{r}} \qquad (2.1)$$

and

$$\frac{P_r - P_o}{P_n - P_o} = 1 \frac{1}{\left\{1 + a\left(\frac{r}{R_c}\right)^2\right\}^b} \dots (2.2)$$

where,

 $P_r = \text{pressure}$  at radial distance  $r_r$ 

 $P_0$  = pressure at the center of hurricane.

 $P_n = \text{pressure at infinite distance.}$ 

 $R_c = \text{radius}$  of maximum

cyclostrophic wind.

The constants  $A = \frac{1}{B}$  and  $a = \frac{1}{b}$  must always be true in order to satisfy the mathematics of the cyclostrophic wind equation. Equation 2.1, proposed by Holland (1980), becomes the original Rankin-Vortex Model when A = B = 1.

Equation 2.2, proposed by Bretschneider (1981) after analysis of the pressure profile data, becomes the BRET-X Model when  $a=\frac{1}{b}=1$  and the same as Fujita model (1962) when  $a=\frac{1}{b}=2$  Table 2.1 presents the theoretical constant K for four hurricane models such as Hydromet Model, NOAA Model-I, Fujita Model-J, and BRET Model-X.

The parameter used to select hurricane models is non-dimensional Rankin-Vortex number,  $N_{CR}$  (Bretschneider and Lo, 1984). The original Hydromet Model is applicable for the low values of  $N_{CR}$  and for the higher values of  $N_{CR}$ , other models might be accepted as shown in Table 2.2. For this study BRET-X Model will be used due to the high latitude of the study site.



For a moving hurricane, the stationary wind field is directly coupled with the corresponding model hurricane wave field and the change in the wind speed component to be corrected as

$$U^*_{RS} = U_{RS} + dU, \cdots (2.7)$$

where dU equals to  $\frac{1}{2}V_f\cos\theta$  and  $\theta$  the angle of wind deflected from the direction of the incurvature angle of the wind speed.

## Equations for Prediction of Hurricane Wave Fields

In general, the wave forecasting or hindcasting can be done either the significant wave method or the wave spectrum mothod. These methods are dedicated by Bretschneider, Burling. Hasselmann (JONSWAP). James. Moskowitz, Montogmery, Munk, mann, Pierson, Rossby. Silvester. Sverdrup, Wilson and so on. For this study, the recent Bretschneider's wave forecasting relationships for constant wind speed and direction, developed sea, and deep water will be used. The significant wave height  $H_s$ and significant wave period  $H_s$  are function of wind speed U, fetch length  $F_{t}$  and wind duration t by use of the  $\cdot$ Buckingham's PHI-theory (1914) and the dimensional analysis as follows

$$\frac{gH_s}{U^2} = A_1 \tanh \left\{ B_1 \left( \frac{gF}{U^2} \right)^{m_1} \right\}, \dots (2.8)$$

$$-\frac{gT_s}{2\pi U} = A_1 \tanh \left\{ B_2 \left( -\frac{gF}{U^2} \right)^{m_2} \right\}, \quad \cdots (2.9)$$

$$t_{min} = 2 \int_{0}^{F_{min}} \frac{1}{C_{o}} dx, \dots (2.10)$$

where.

$$A_1 = 0.283, B_1 = 0.0125, m_1 = 0.42,$$

$$A = 1.200$$
,  $B = 0.0770$ ,  $m_2 = 0.25$ ,

U=10-minute average surface wind speed at 10-meter above the water level.

 $C_0$  = wave celerity in deep water.

The parameters and constants are based on foot scale.

The model wave height field for stationary hurricane developed by Bretschneider (1972) shows

$$H_c = H_R \left(1 + \frac{1}{2} \frac{V_f \cos \theta}{U_{Rs}}\right)^2$$
, .....(2.12) where,  $\theta$  is an angle between the direction of wind and the forward moving direction of hurricane. The model wave period field can be derived as follows after eliminating fetch term  $F$ , using the above coefficients and

 $T_R = 0.4 U_{Rs} \tanh \left\{ 1.07 \left( \tanh^{-1} 40 \frac{H_R}{U_{Rs}^2} \right)^{0.6} \right\}.$ 

expressing U in knots and g as 32.2

Modified significant wave period for moving hurricane shows

$$T_c = T_R \left(1 + \frac{1}{2} \frac{V_f \cos \theta}{U_{Rs}}\right)^2 \cdots (2.14)$$

and the forward speed can vary from  $V_f=0$  to  $V_f=C_s=1.515\,T_c$ , where  $C_s$  is the group velocity of the significant waves. The upper limit of  $V_f=C_s=20$  to 25 knots (Bretschneider, 1986) after the hurricane



moves faster than the waves it has generated, producing very confused seas, and the results might be in doubt. Thus, for calculation by a computer program in this study it is assumed that the forward speed  $V_j = C_s \leq V_{C_s}$  the critical forward speed.

All these calculations for significant typhoons passed by the Korean Peninsula since 1947 were done by the IBM PS/2 386 (20MHz) in order to predict the 100-year typhoon characteristics and results will be discussed later.

## Calculation of the 100-Year Design Wave Parameters

## 3.1. Description of Study Area

Youngil Bay is located at southern part of the east coast of Korean peninsula (36°-03'N, 129°-23'E) and has about 10Km width of bay entrance, an open northeastly to the East Sea (Japan Sea) and 15km length and a concaved form southwestly as shown in Figure 3. 1. Inside the bay, there are two harbors, Pohang Old Harbor and Pohang New Harbor. There is a river between these two harbors. This bay includes not only the industrial complex such as the Pohang Steel Company and its sub-industrial companies which are the vital part of the heavy-chemical industry development of Korea but also Songdo Beach which gives a rest place for the civilians and a resort area for the tourists.

The depth is abruptly decreasing from the open sea to the bay. The average depth of the bay is 21m and the distribution of the contour lines is similar to the shape of the bay. Bottom profile at the cross-section A-A' shows Figure 3.2. The bottom profile had been changed significantly year by year and is still changing due to the dredging work in connection with the construction of a new harbor to assist the industrial complex. Moreover, since 1970 the site has frequently been exposed to beach erosion and damages on the shore structures from severe storms.

## 3.2. Calculation of Typhoon Parameters

In order to calculate typhoon parmeters typhoon data were collected in three steps:

- a) all typhoons which were within 325 n. miles (CPTT; the Closest Point of Typhoon Track) from the study site between 1961 and 1985 were collected to calculate  $V_c$  and  $R_c$  with models decided by Rankin-Vortex Number ( $N_{CR}$ ) as described in Chapter 2,
- b) pressure  $(P_0)$ , latitude  $(\phi)$ , forward speed  $(V_0)$  and maximum wind  $(V_{OMAX})$  were collected at locations which the closest point to the study area keeping the typhoon intensity, within 350 n. miles (CPTI; the Closest Point of Typhoon Intensity),
- c) to get the worst situation from the data recorded, it is assumed that the typhoon intensity continues to CPTT.



In case of the typhoon is moving at a forward speed  $V_i$ , and for a completely undamped system, the response factor R takes on the following form

$$R = -\frac{gh}{(V_f^2 - g\triangle h)} \cdots (4.3)$$

The elevation becomes very great and there is a resonace. But the frictional and damping factors will prevent a complete free resonance. Thus,

$$S_P = 1.14(1)(1-e^{-1.28}) = 0.4 ft (12.19 cm).$$

From the computer simulation for typhoon Brenda this can be derived.

Wind Setup 
$$(S=S_x+S_y)$$

The rise in water level caused by the wind stress component directed perpendicular to the coast, wind tide  $S_{x}$ , is a function of wind speed, direction and water depth.

The most significant wind direction at Youngil Bay is WSW which is 51.7% of al wind directions. The next one is NNE direction. N, NNE and NE directions are 23.1% and the rest, 25.2%. Among the wind directions over 10m/sec of wind speed, NNE wind is 40.2% of all directions and N, NNE and NE winds, 67.8%, whereas W, WSW and SW winds are only 25.3%.

The rise (or drawdown) of water level due to the wind stress component parallel to the coast, Coriolis tide  $S_{*}$ , caused by a current following parallel to the coastline.  $S_{*}$  can exist in the absence of any wind when a hurricane has no wind.

With the assumption for bathystrophic approximation, quasi-steady state (nearly constant wind speed) and constant bottom slope, the following equations for  $S_{\mathbf{z}}$  and  $S_{\mathbf{y}}$  developed by bretschneider (1967) are applicable to determine the wind setup near the coastline.

$$S_x = kU^2 \frac{\cos \theta'}{g} G_0, \quad \dots (4.4)$$

$$S_y = \frac{6}{7} \frac{fUF}{g} \sqrt{\frac{k}{K' \sin \theta'}} D_0^{\frac{1}{6}}, \quad \dots (4.5)$$

Where.

$$G_o = \frac{F}{D_o - (D_c + S)} \ln \left( \frac{D_o}{D_c + S} \right),$$

k=surface wind stress parameter, 3.0×10<sup>-6</sup>(Saville)

K = bottom friction parameter,  $10^{-2}$  (shallow water).

 $\theta^{i}$  =direction of wind, angle from the line perpendicular to the coast.

S=total wind setup,

Do=breakoff end of the slope at the edge of the continental shelf,

 $D_c$ =depth at the coast.

 $G_0$  is solved as a function of fetch distance offshore, corresponding water depth, and an arbitrary water depth near the shoreline. Based on the bottom profile as Figure 3.2, it was assumed that  $D_0+S=1.5m$ . computation of  $G_0$  shows Figure 4.1 and a maximum  $G_0$  of 0.232(n. miles/ft) was determined at a distance offshore of 13n. miles corresponding to a water depth  $D_0$  of 66m (216.5ft).

Computer program uses above equations for  $S_{\mathbf{z}}$  and  $S_{\mathbf{y}}$  to calculate the



11

wind setup (S). However, we can use modified equations

$$S_x = 6080 \frac{k}{g} \frac{U^2}{30} \cos \theta G_o$$
$$= 1.456 \frac{U^2}{30} \cos \theta G_o$$

and

$$S_y = 0.05490 \frac{U}{30} \sin \phi \ D_o^{\frac{1}{6}} \sqrt{\sin \theta}$$

$$=\pm 0.1940 \frac{U}{30} \sqrt{\sin \theta}$$
, at  $\phi = 36.0$ °N

= 
$$\pm 0.1719 \frac{U}{30} \sqrt{\sin \theta}$$
, at  $\phi = 31.4$ °N.

The value of  $S_{\nu}$  differed slightly for two different latitudes and the value for 31.4°N was chosen to calculate wind setup. Calculated manimum wind setups by the computer at 45n miles of CPTT for Brenda are 41.64cm for  $S_{\nu}$  and -7.96cm for  $S_{\nu}$ 

## Wave Setup $(S_w)$

As deep water waves encounter a sloping shelf, they become short, steep and finally break, while travel forward after breaking. The increase in the mean stil water near the beach due to the effect of breaking waves is known as wave setup. The computer simulation shows the maximum wave setup at the study srea as 137.16cm (4.5ft) as shown in Figure 4.2.

Summary of Total Design Water Depth  $(D_i)$ 

Again the resultant total design water depth is

$$D_t = D_{MLLW} + A_s + S_p + S_x + S_y + S_w;$$
  
= 5. 0000 + 0. 1040 + 0. 1219 + 0. 4164  
- 0. 0796 + 1. 3716 \approx 6. 93m.

Figure 4.3 shows the observed sea surface fluctuation during the passage of typhoon Brenda. The mean tide level at Youngil Bay is 12.0cm from the datum level. On October 6, the maximum storm surge was recorded with 32.0cm from the mean tide level. If this was recorded at the ebb tide, the maximum will be 42.4cm. This value is very close to the value of the predicted storm surge, 45.1cm. Table 4.1 shows an example of the calculation of the storm surge.

## 5. Summary and Discussions

Various typhoon data since 1961 for the study site were collected and analyzed with some criteria. Derived parmeters were introduced into calculation of total design water depth. The method used in this study for determination of typhoon parameters is limited to a hurricane or typhoon intensity whose moving speed equals to or less than its critical forward speed. Thus, those typhoons faster than this limit need further study.

Storm surge inside the Youngil Bay will be higher than the calculation because of the concaved shape of the bay and the seiche motion.

This study gives the methods for calculating typhoon winds, waves and total design water depth. In order to create a final and optimum design, more study on the environmental condition such as the current and near shore littoral process supported by the hydraulic



model experiment, and a rigorous economic analysis should be followed. Moreover, we need steps for shallow water design wave and wave run up calculations. This is beyond the scope of this study and this will be followed by the next paper.

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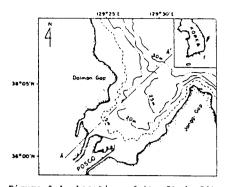


Figure 3.1 Location of the Study Site and Depth Profile

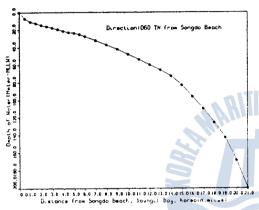


Figure 3.2 Bottom Profile in and Out of Youngil Bay, Korea

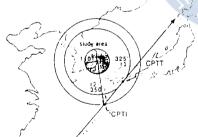


Figure 3.3 Typhoon Data Collection from 1961 to 1985

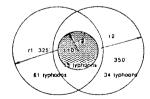


Figure 3.4 Selection of Typhoons to Calculate the Return Period

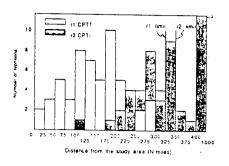


Figure 3.5 Distribution of 61 Typhoons

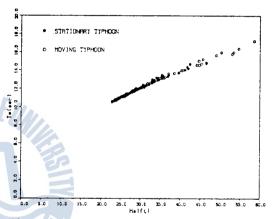


Figure 3.6 Relationship between  ${\rm H_S}$  and  ${\rm T_S}$  for Stationary Case and Moving Case

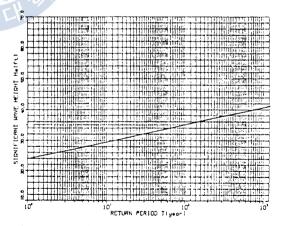


Figure 3.7 Plot of the Significant Wave Height versus Return Period from Analysis of Typhoon Data



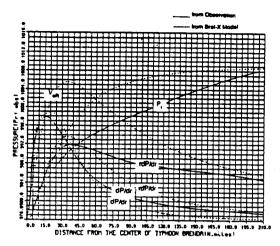


Figure 3.8 Plot of Typhoon Brenda (1985) Parameters from Observation and Bret-X Model

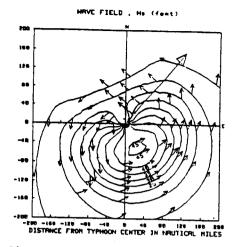


Figure 3.10 Calculated Wave Height Field for Typhoon Brenda

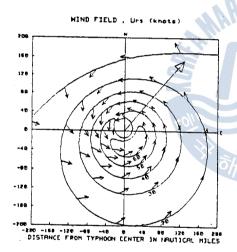


Figure 3.9 Calculated Wind Field for Typhoon Brenda

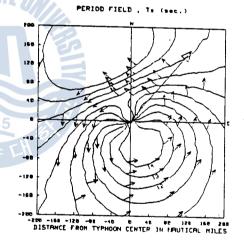


Figure 3.11 Calculated Wave Period Field for Typhoon Brenda



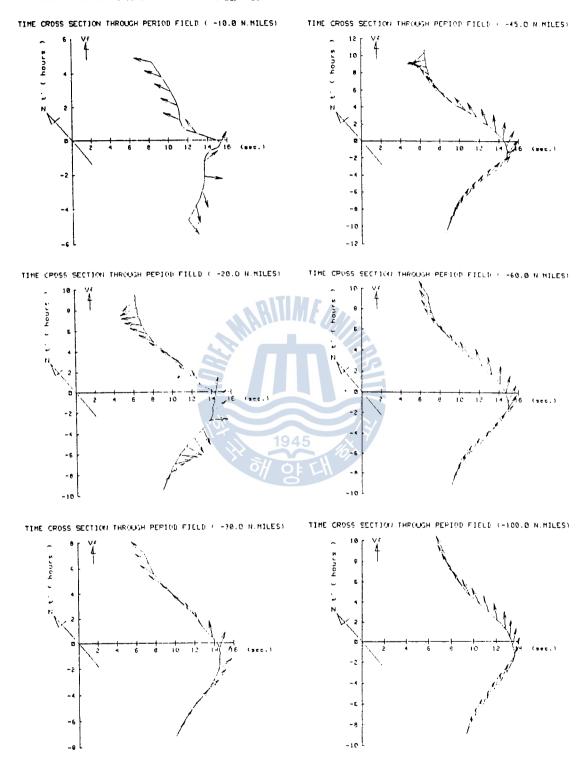


Figure 3.14 Time Cross Sections through the wave Period Field

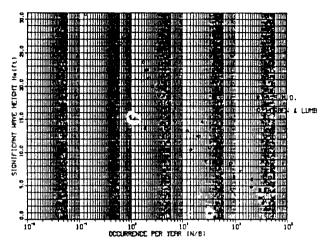


Figure 3.15 Occurrence per Year versus Significant Wave Height from S.S.M.O. and Hogben & Lumb's Data

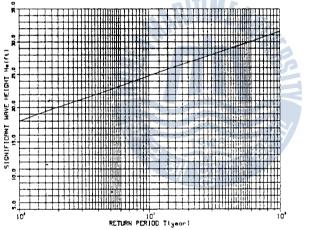


Figure 3.16 Plot of the Significant Wave Height Versus Return Period from S.S.M.O. and Hogben & Lumb's Data

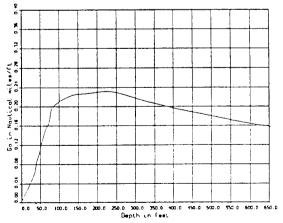
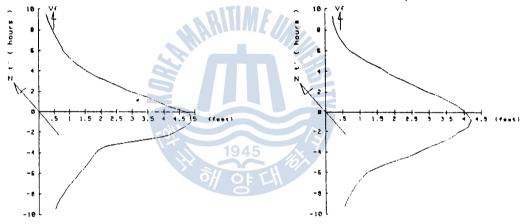


Figure 4.1 Plot of  $G_0$  versus  $D_0$  for the Traverse A-A' of Youngil Bay, Korea



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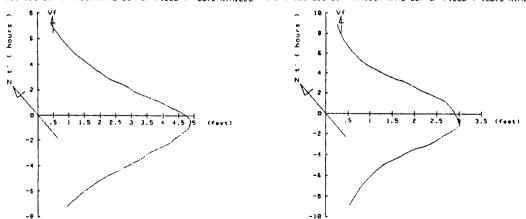


Figure 4.2 Time Cross Sections through the Wave Setup Field



Table 4.1 Storm Surge Calculation

TYPHOON : BRENDA

Lat. = 31.4 deg.; Rc= 35.09 n.mi.; Po= 33.3 mbs: Vf= 23.68 knts; Dir. = 40 deg.

×	t ′	Ur s	£u.	Bh	Pr '' Hg		Sp FEET	S× FEET	Sy FEET	
н.м.		KHOTS	DEG	DEG	-					
	-6.968			249.7 250.4	29.800 29.878		.045 .047	.183	.026 .023	
	-6.757 -6.546			250.4	29.876		.050	. 209	.019	
-155.0 -150.0	-6.334	24.4		252.1	29.873		.053	.223	.013	
-145.0	-6.123	25.2		252.8	29.870		.056	. 239	007	
-140.0	-5.912	26.1		253.6	29.867		.060		018 026	
-135.0	-5.701	27.0		254.4	29.864 29.860		.064 .068	.274 .294	032	
-130.0	-5.490	28.0 29.0	252.8 252.7	255.1 255.0	29.856		.072	.316	038	
-125.0 -120.0	-5.279 -5.068	30.1	252.6	256.4	29.851		.077	.339	044	
-115.0	-4.856	31.2	252.4	257.8	29.847		.083	.365	051	
-110.0	-4.645	32.5	252.1	257.7	29.841		.089	.394	058 066	
-105.0	-4.434	33.9	251.6	258.4	29.835		.096 .103	.427 .467	075	
-100.0	-4.223	35.4	251.4 250.9	259.2 260.2	29.829 29.821		.111	.513	086	
-95.0 -90.0	-4.012 -3.801	37.2 39.2	250.4	261.4	29.813		.120	.567	098	
-85.0	-3.598	41.3	249.7	262.5	29.804		.131	.626	111	
-80.0	-3.378	43.5	248.8	263.4	29.795		.142	.688	125	
-75.0	-3.167	45.6	247.8	263.9	29.784		.154	.751 .809	138 149	
-70.0	-2.956	47.5	246.6	264.0	29.772 29.758	IM <i>t</i>	.183	.854	158	
-65.0	-2.745 -2.534	49.0 49.9	245.1 243.4	263.6	29.743		.200	.882	165	
-60.0 -55.0	-2.323	51.2	241.4	262.1	29.727		.218	. 921	174	
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-45.0	-1.900	57.0	237.0	262.3	29.691		.259	1.103	214 225	
-40.0	-1.689	58.9	234.2	260.5	29.671 29.650		. 282	1.165	241	
-35.0	-1.478	61.1	231.0	259.2 258.4	29.629			1.258	256	
-30.0 -25.0	-1.267 -1.056	62.3 62.7	223.5	254.8	29.608		.352	1.261	259	
-50.0	845	64.7	219.1	248.8	29.503		.374	1.366	261	
-15.0	633	64.5	214.3	245.4	29.572		.393	1.336	265 268	
-10.0	422	64.4	209.2	241.2	29.559		.408	1.320	271	
-5.0	211	64.2	203.9	236.8	29.551 29.548	945	.420	1.272	273	
0.0 5.0	0.000 .211	63.8 63.4	198.4 192.8	227.4	29.551		.417	1.244	274	
10.0	. 422	63.0	187.4	222.6	29.559	2651	.408	1.217	274	
15.0	.633	62.4	182.2	218.0	29.572		.393	1.185	274	
20.0	. 845	62.1	177.2	213.8	29.589		.374	1.172	272 273	
25.0	1.056	59.5	172.9	212.8	29.608 29.629		.329	.967	273	
30.0	1.267	58.6 57.0	168.7 165.1	204.7	29.650		.305	.939	261	
35.0 40.0	1.689	54.4	161.9	200.9	29.671		.282	.865	248	
45.8	1.900	52.3	159.1	198.9	29.691		.259	.790	240	
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55.0	2.323	46.1	155.0	191.7	29.727		.218	.639 .601	197	
60.0	2.534	44.6	153.0	189.5	29.743 29.758		.183	.569	193	
65.0 70.0	2.745 2.956	43.5 42.0	151.2	187.0	29.772		. 168	. 526	187	
75.0	3.167	40.0	148.7	185.7	29.784		. 154	.478	178	
80.0	3.378	37.8	147.9	183.8	29.795		.142	.433	166 153	
85.0	3.590		147.3	181.5			.131	.354	139	
90.0	3.801	33.3	146.9	178.9 176.4			.111	.329	126	
95.0	4.012		146.6	174.5			.103	.289	116	
100.0 105.0	4.434			173.2	29.835		.096	. 261	187 100	
110.0	4.645		146.6	172.4			.089	.237 .216	095	
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120.0			146.9				.072	. 180	087	
125.0			_				.068	. 164	084	
130.0 135.0				174.7			. 964	. 150		
140.0	_				29.867		.060			
145.0	6.123	19.3					.056 .053			
150.0							.050			
155.0							.047			
160.0	6.75						.045			
165.0	6.96	8 15.4								





