

# Dynamic Stability of Damaged Ship in Random Beam Seas

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## ABSTRACT

This paper presents a brief outline of dynamic stability of damaged ship at final stage of flooding in rough, beam wind and waves. First of all, we evaluate the static, residual stability of damaged ship. Then we also evaluate the dynamic stability of damaged ship in terms of capsizing probability based on energy balance in roll and risk analysis, the method of which was firstly proposed by Umeda et al.(1993) to high speed craft in intact condition. The one degree-of-freedom roll equation is adopted with effects of damage fluid and external forces due to wind and waves, but without effect of sloshing. As a result, we can express the dynamic stability of damaged ship in probabilistic manner according to sea state, operating condition and damage situation.

## 1. INTRODUCTION

Capsizing of damaged ship may happen due to deficiency of pure static, residual stability, but also more frequently due to deficiency of dynamic stability in rough weather. For safety against capsizing of intact ship due to deficiency of dynamic stability in beam seas, Resolution A.562, weather criterion, was recommended by IMO(1985). The criterion was based on energy balance in roll motion with experientially determined safety factor. So it can hardly be justifiable to apply the criterion directly to damaged ship. Recently Umeda et al.(1993) have pointed out that IMO Resolution A.562 has several problems from the viewpoint of modern naval architecture, then have suggested risk analysis method for assessment of dynamic stability of intact ship in beam seas.

In this paper, we establish dynamic stability assessment of damaged ship at final stage of flooding in rough, beam wind and waves. The degree of dynamic stability of damaged ship is expressed quantitatively in terms of capsizing probability that is calculated on the basis of the theory of ship dynamics with the effect of sea state, operating condition and damage situation. These probabilistic method was firstly applied by Umeda et al.(1993) to high speed crafts in intact condition. Before application of the probabilistic method to the assessment of dynamic stability of damaged ship, we also establish residual static stability of damaged ship on the basis of lost buoyancy method and added weight method(Lewis(1988)). The present study was carried out as a part of rescue technique of damaged ship.

## 2. METHOD

### 2.1 Residual static stability

Fig. 1 shows that the ship initially at waterline  $WL_1$ , comes to float at waterline  $WL_2$  because of sinkage and trim due to flooding of one or more of its compartments. According to lost buoyancy method(Lewis(1988)), we can evaluate the equilibrium draft after flooding as follows.

$$\begin{aligned} df &= df_0 + S - (0.5 - LCF_1'/L) t \\ da &= da_0 + S + (0.5 + LCF_1'/L) t \end{aligned} \quad (1)$$

where  $L$  denotes ship length,  $df$  and  $da$  fore and aft drafts at waterline  $WL_2$ ,  $df_0$  and  $da_0$  those at waterline  $WL_1$ ,  $S$  and  $t$  parallel sinkage and change in trim due to damage fluid, and  $LCF_1'$  the center of flotation of remaining area of impaired waterplane  $WL_1$  from amidships. According to added weight method(Lewis(1988)), we can also evaluate the metacentric height  $GM_2$  at waterline  $WL_2$ . Using the numerical calculation method suggested by Hamamoto(1993), we calculate the static righting arm  $GZ_2$  for the metacentric height  $GM_2$  at waterline  $WL_2$ .

Then the effective righting arm corresponding to waterline  $WL$ , denoted as  $GZ'$ , can be expressed as follows.

$$GZ' = GZ_2 \times W_2 / W \quad (2)$$

where  $W$  denotes displacement before flooding, and  $W_2$  that after flooding, which containing damage fluid.

Fig. 2 shows heeling moment and heel angle due to unsymmetrical flooding. For final stage of flooding, the residual static righting arm  $GZ$  will be evaluated as follows.

$$GZ = GZ' - \delta v' (tcg - TCG) \cos \phi / W \quad (3)$$

where  $\delta$  denotes specific weight of damage fluid,  $v'$  net volume of damage fluid below waterline  $WL$ ,  $\phi$  heel angle, and  $tcg$  and  $TCG$  transverse center of gravity of  $v'$  from amidships and that of net added buoyancy from amidships respectively.

## 2.2 Sea states

We assume that wind velocity changes with time around average velocity  $U_T$  according to wind spectrum suggested by Davenport(1957). Further it is also assumed that the wind generates long crested irregular waves on sea surface with significant wave height  $\bar{H}_{1/3}$  and mean wave period  $\bar{T}$  as given in Table 1 for corresponding values of Beaufort scale. Standard spectrum recommended by ITTC(1978) for fully developed waves, is determined to be used here.

## 2.3 Roll equation and response spectrum

The roll motion of damaged ship drifting in beam wind and waves is considered. Firstly the static heel angle,  $\phi_s$ , caused by aerodynamic lateral force,  $F_A$ , is obtained by the following equation of equilibrium(cf. Fig. 3).

$$F_A (h_A + h_H) - WGZ(\phi_s) = 0 \quad (4)$$

where  $h_A$  and  $h_H$  denote the distances from waterline to the center of projected area in air and to that of drifting force in water respectively, and  $GZ$  the residual static righting arm of damaged ship.  $F_A$  is given as follows

$$F_A = \frac{1}{2} \rho_A A_A C_{DA} U_T^2 \quad (5)$$

where  $\rho_A$  denotes air density,  $A_A$  projected area of damaged ship in air,  $C_{DA}$  aerodynamic drag coefficient. For the roll motion of damaged ship in inclined condition due to static heel angle, referring to papers by Shin(1981), Tasai(1969) and Kat(1996), we adopt one degree-of-freedom roll equation with the effects of damage fluid and external forces, but without sloshing effect as follows.

$$(I_{xx} + J_{xx}) \ddot{\phi}_r + B_e \dot{\phi}_r + WGM_s \phi_r = WGM_s \gamma \Theta_w(t) + \tilde{K}_A(t) \quad (6)$$

where  $(I_{xx} + J_{xx})$  denotes virtual moment of inertia in roll,  $B_e$  equivalent linear damping coefficient,  $\phi_r$  relative roll angle measured from  $\phi_s$ , namely  $\phi_r = \phi - \phi_s$ ,  $GM_s$  the slope of residual  $GZ$  curve of damaged ship at static heel angle  $\phi_s$ , namely  $GM_s = [dGZ/d\phi]_{\phi=\phi_s}$ ,  $\gamma$  effective wave slope coefficient,  $\Theta_w(t)$  instantaneous slope of surface waves, and  $\tilde{K}_A(t)$  instantaneous roll moment due to fluctuating wind velocity, denoted as  $u(t)$ , which is assumed as  $|u(t)| \ll U_T$ .  $\tilde{K}_A(t)$  is given as follows.

$$\tilde{K}_A(t) = \rho_A A_A C_{DA} h_{AG} U_T u(t) \quad (7)$$

where  $h_{AG}$  is the distance of center of the wind force from center of gravity of damaged ship. The eq. (6) may be replaced by another form as follows.

$$\ddot{\phi}_r + b_e \dot{\phi}_r + \omega_s^2 \phi_r = \omega_s^2 \gamma \Theta_w(t) + k_A u(t) \quad (8)$$

where

$$\omega_s^2 = WGM_s / (I_{xx} + J_{xx}) \quad (9)$$

$$k_A = \rho_A A_A C_{DA} h_{AG} U_T / (I_{xx} + J_{xx}) \quad (10)$$

# 원문누락

원문누락

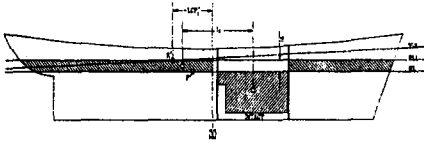


Fig. 1 Sinkage and change in trim caused by lost buoyancy

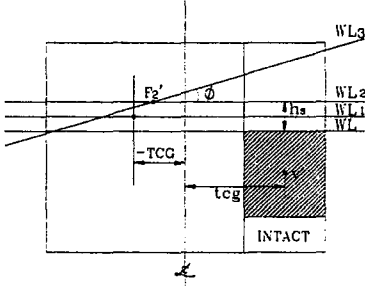


Fig. 2 Unsymmetrical flooding and heel

Table 1 Sea states

Beaufort	$U_T$ (m/sec)	$\bar{H}_{1/3}$ (m)	$\bar{T}$ (sec)
1	0.95	0.1	1.2
2	2.50	0.2	1.7
3	4.45	0.6	3.0
4	6.75	1.0	3.9
5	9.40	2.0	5.5
6	12.35	3.0	6.7
7	15.55	4.0	7.7
8	19.00	5.5	9.1
9	22.65	7.0	10.2
10	26.50	9.0	11.6
11	30.60	11.5	13.1
12	34.85	14.0	14.4

Table 2 Principal dimensions of ship and model

Items	Ship	Model
Length between perpendiculars $L$ (m)	167.0	2.385
Breadth $B$ (m)	22.6	0.323
Depth $D$ (m)	13.4	0.191
Mean draft (designed) $d$ (m)	9.0	0.1287
Displacement volume $V$ ( $m^3$ )	26186.0	0.0763
Block coeff. $C_b$	0.77	0.770
Prismatic coeff. $C_p$	0.778	0.778
Waterplane coeff. $C_w$	0.849	0.849
Model scale		1/70

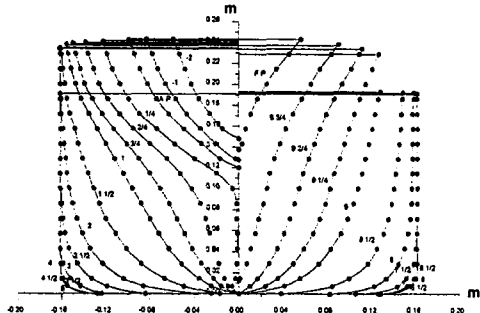


Fig. 4 Body plan (numerical value is expressed in model size)

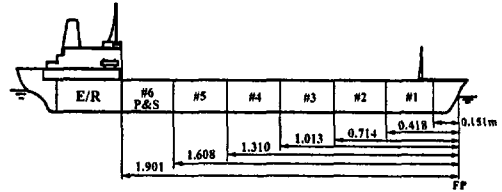


Fig. 5 Profile and tank arrangement (numerical value is expressed in model size)

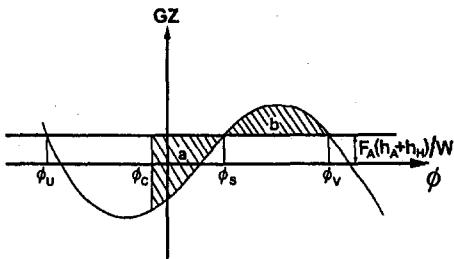


Fig. 3 Energy balance in roll

Table 3 Definition of damage number

Damage No.	Damaged tank
-1	#6 port
1	#6 star.
2	#5
3	#4
4	#3
5	#2
6	#1
7	#6 port & star.
8	#6 port & #5
9	#6 star. & #5
10	#5 & #4
11	#4 & #3
12	#3 & #2
13	#2 & #1

Table 4 Intact condition of full ship

Ballast condition		
Draft fore	df	3.71 m
aft	da	4.41 m
Metacentric height	GM	3.1, 2.5, 2.0 m
Permeability	$\mu$	0.95
	$\mu_s$	0.97
Half load condition		
Draft fore	df	6.0 m
aft	da	7.0 m
Metacentric height	GM	1.0, 0.7 m
Permeability	$\mu$	0.5
	$\mu_s$	0.5

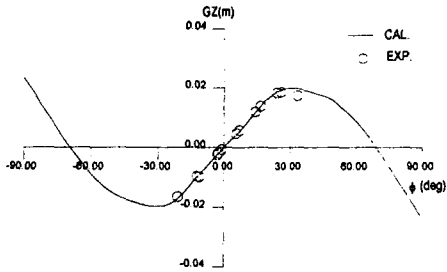


Fig. 6 Righting arm at intact condition(ballast condition,  $GM = 3.1 m$  in full size)

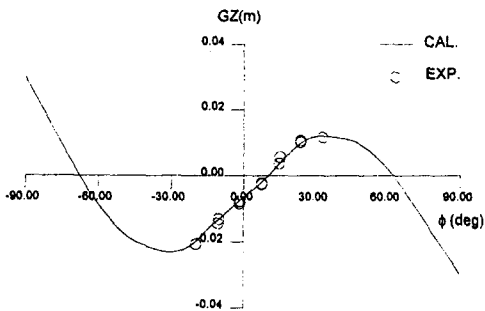


Fig. 7 Residual righting arm for damage No. 1 (ballast condition, initial  $GM = 3.1 m$  in full size)

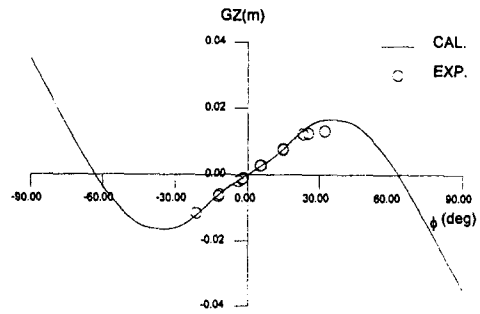


Fig. 8 Residual righting arm for damage No. 2 (ballast condition, initial  $GM = 3.1 m$  in full size)

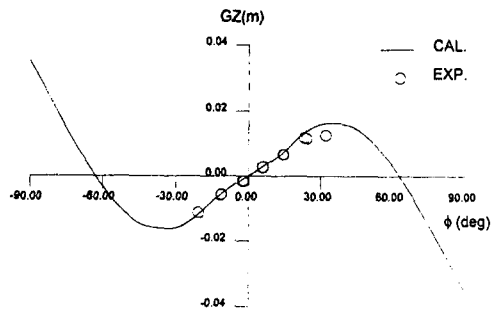


Fig. 9 Residual righting arm for damage No. 4 (ballast condition, initial  $GM = 3.1 m$  in full size)

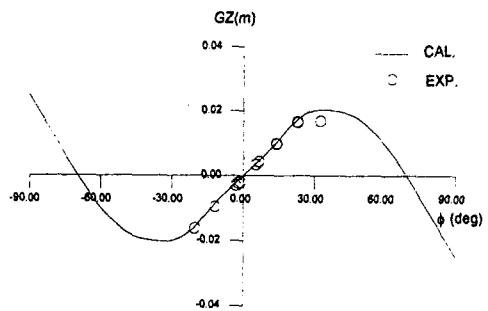


Fig. 10 Residual righting arm for damage No. 6 (ballast condition, initial  $GM = 3.1 m$  in full size)

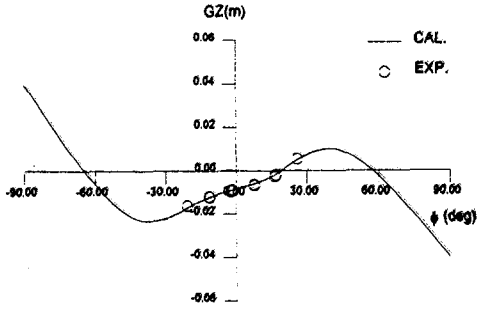


Fig. 11 Residual righting arm for damage No. 9 (ballast condition, initial  $GM = 3.1 m$  in full size)

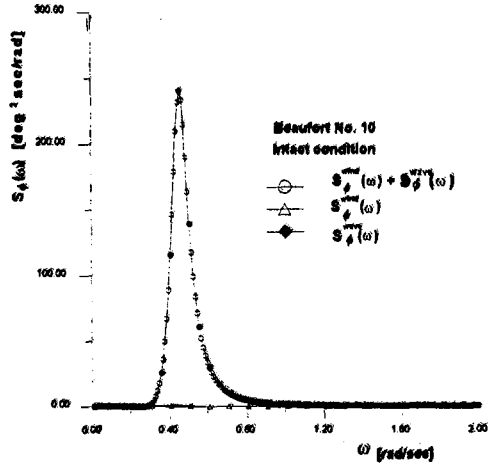


Fig. 14 Roll response spectrum (ballast condition, initial  $GM = 2.0 m$ )

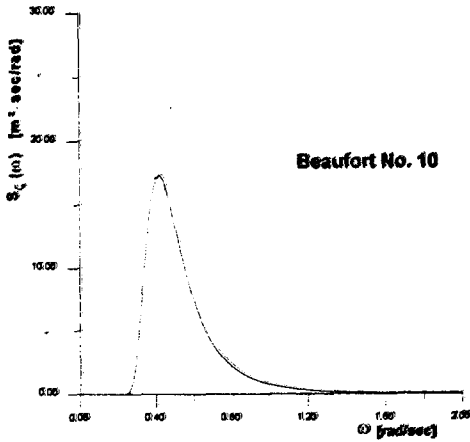


Fig. 12 ITTC(1978) wave spectrum

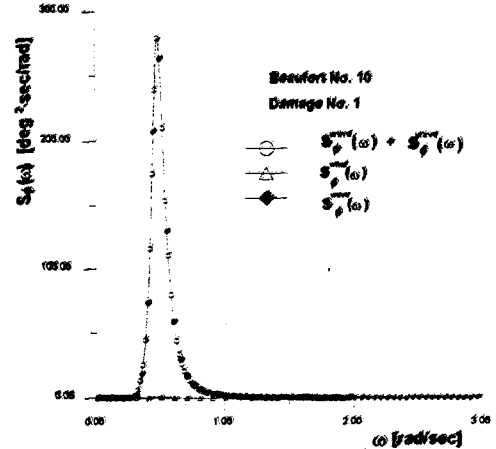


Fig. 15 Roll response spectrum (ballast condition, initial  $GM = 2.0 m$ )

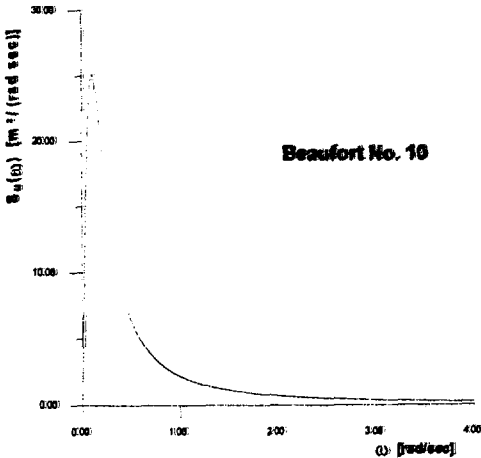


Fig. 13 Davenport wind spectrum

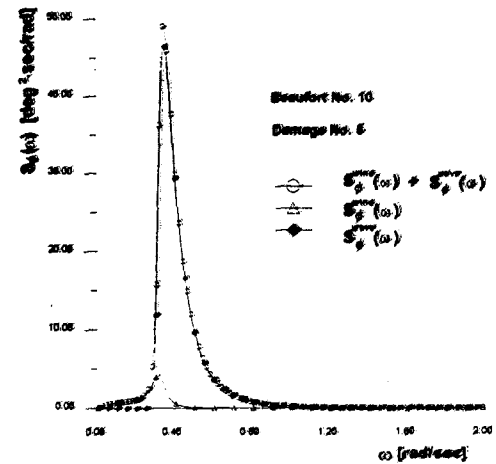


Fig. 16 Roll response spectrum (ballast condition, initial  $GM = 2.0 m$ )

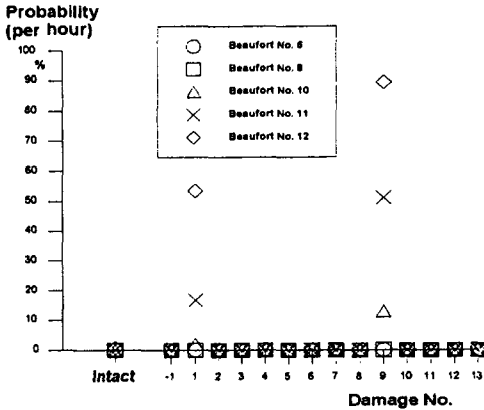


Fig. 17 Capsizing probability per hour(ballast condition, initial  $GM = 3.1 m$ )

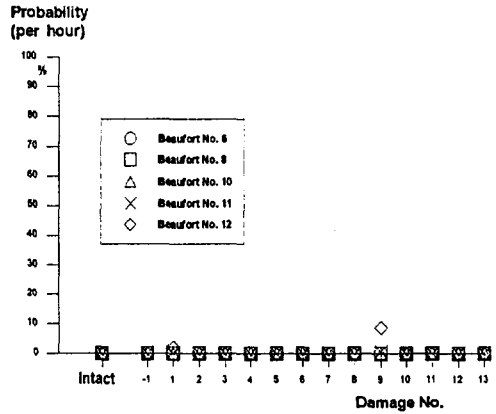


Fig. 20 Capsizing probability per hour(half load condition, initial  $GM = 1.0 m$ )

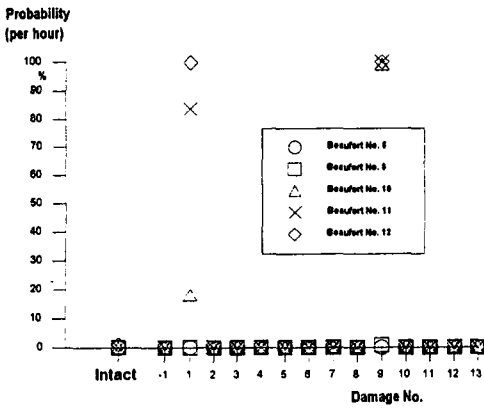


Fig. 18 Capsizing probability per hour(ballast condition, initial  $GM = 2.5 m$ )

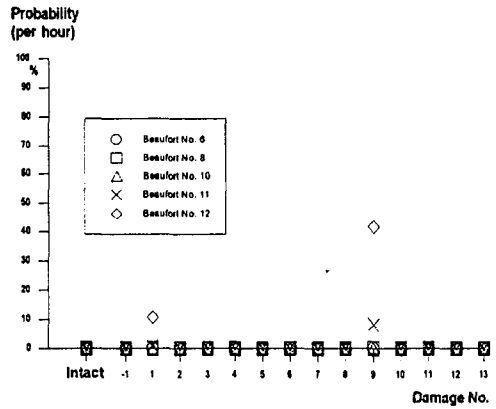


Fig. 21 Capsizing probability per hour(half load condition, initial  $GM = 0.7 m$ )

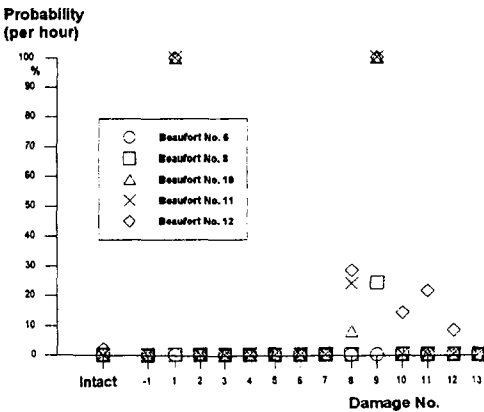


Fig. 19 Capsizing probability per hour(ballast condition, initial  $GM = 2.0 m$ )